

## < 4.10 The Vortex Panel Method >

### \* Thin airfoil theory

- Closed form
- Limited to thin airfoil,  $\frac{t_{\max}}{c} \leq 12\%$

### \* Panel method

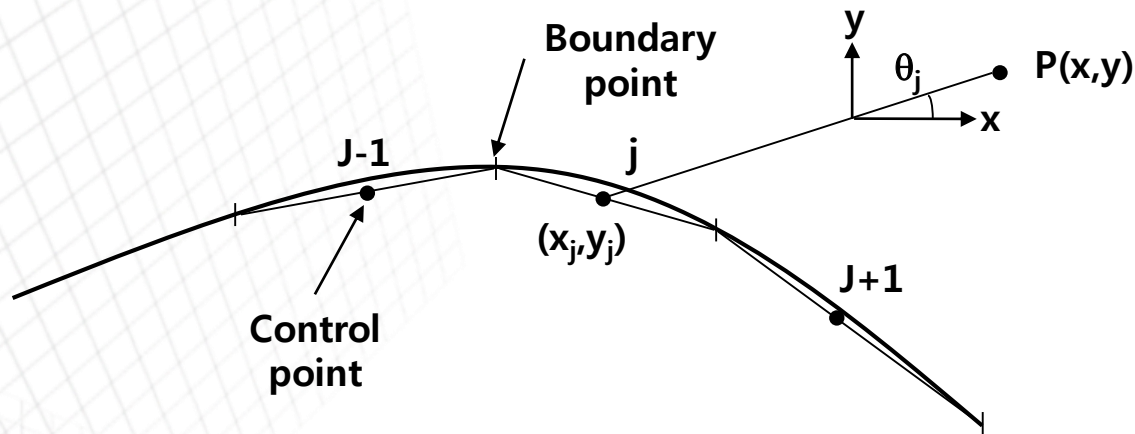
\_2017

- Vortex panel
- Source panel → non-lifting cases

- \* Exactly same idea of thin airfoil theory, but no closed form  $\gamma(s)$   
→ solve numerically

# Incompressible Flow over Airfoils

## < 4.10 The Vortex Panel Method >



\* The velocity potential at P due to j-th panel

$$\Delta\phi_i = -\frac{1}{2\pi} \int_j \theta_{pj} \gamma_j ds_j \quad \Rightarrow \quad \phi(p) = \sum_{i=1}^n \phi_j = -\sum_{i=1}^n \frac{\gamma_j}{2\pi} \int_j \theta_{pj} ds_j$$

$$\theta_{pj} = \tan^{-1} \frac{y - y_j}{x - x_j}$$

\* Let's put point P at the control point of i-th panel

$$\phi(x_i, y_i) = -\sum_{j=1}^n \frac{\gamma_j}{2\pi} \int_j \theta_{ij} ds_j \quad \text{where } \theta_{ij} = \tan^{-1} \frac{y_i - y_j}{x_i - x_j}$$

# Incompressible Flow over Airfoils

## < 4.10 The Vortex Panel Method >

\* At the control points, the normal component of velocity is zero.

- The component of  $V_\infty$  normal to i-th panel

$$V_{\infty,n} = V_\infty \cos \beta_i$$

- The normal component of induced velocity at  $(x_i, y_i)$

$$\begin{aligned} V_n &= \frac{\partial}{\partial n_i} [\phi(x_i, y_i)] \\ &= - \sum_{j=1}^n \frac{\gamma_j}{2\pi} \int_j \frac{\partial \theta_{ij}}{\partial n_i} ds_j \end{aligned}$$

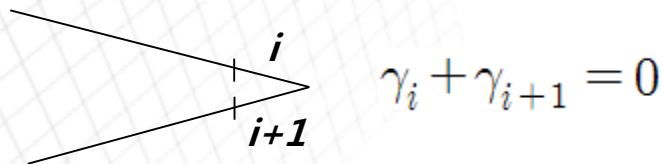
$$\begin{aligned} \rightarrow V_{\infty,n} + V_n = 0 \quad \rightarrow \quad V_\infty \cos \beta_i - \underbrace{\sum_{n=1}^{\infty} \frac{\gamma_j}{2\pi} \int_j \frac{\partial \theta_{ij}}{\partial n} ds_j}_{= J_{ij}} = 0 \\ = J_{ij} : \mathbf{f} \text{ (panel geometry)} \end{aligned}$$

# Incompressible Flow over Airfoils

## < 4.10 The Vortex Panel Method >

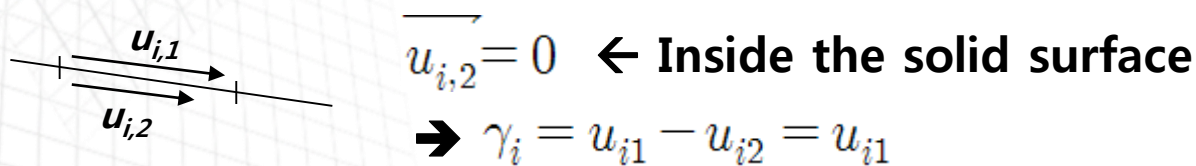
\* Boundary condition : 
$$V_\infty \cos \beta_i - \sum_{n=1}^{\infty} \frac{\gamma_j}{2\pi} \int_j \frac{\partial \theta_{ij}}{dn} ds_j = 0$$

+ Kutta condition :



\* Now, we have (n+1) eq. with n unknowns  $\rightarrow$  ignore one of control points

\* The flow velocity tangent to the surface =  $\gamma$



\* Total circulation : 
$$\Gamma = \sum_{j=1}^n \gamma_j s_j$$

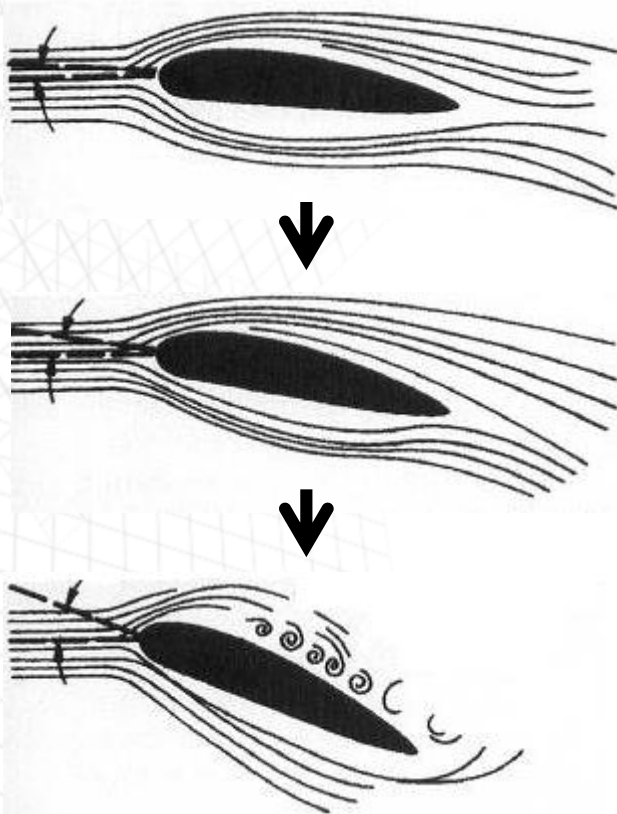
\* Lift : 
$$L = \rho_\infty V_\infty \sum_{j=1}^n \gamma_j s_j$$

# Incompressible Flow over Airfoils

## < 4.12 The Flow over an Airfoil – the Real Case >

### ❖ Stall

- Leading-edge stall



Flow separation takes place over the entire top surface of the airfoil after occurring at the leading edge

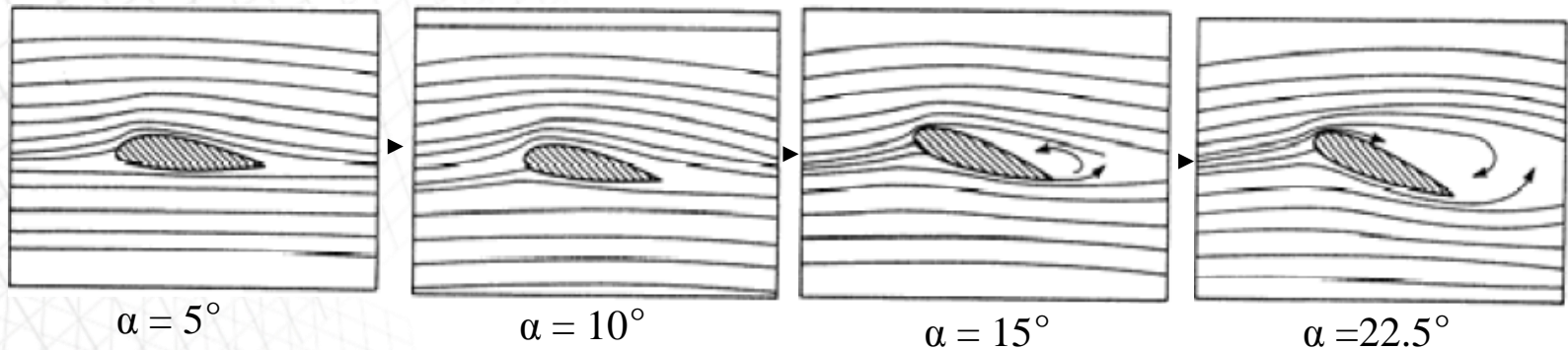


# Incompressible Flow over Airfoils

## < 4.12 The Flow over an Airfoil – the Real Case >

### ❖ Stall

#### ● Trailing-edge stall

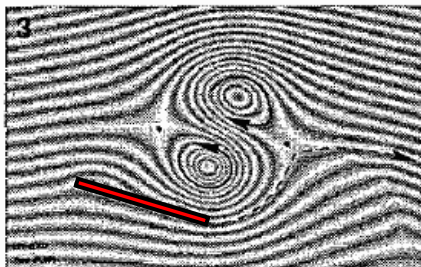
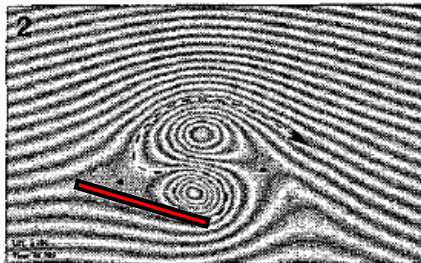
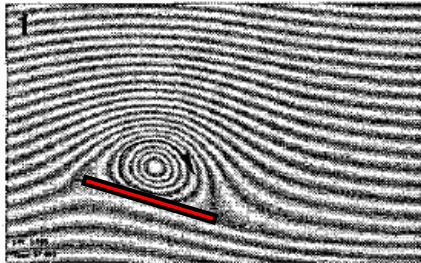


Flow separation takes place from the trailing edge at thicker airfoils than leading-edge stall

## < 4.12 The Flow over an Airfoil – the Real Case >

### ❖ Stall

- Thin airfoil stall



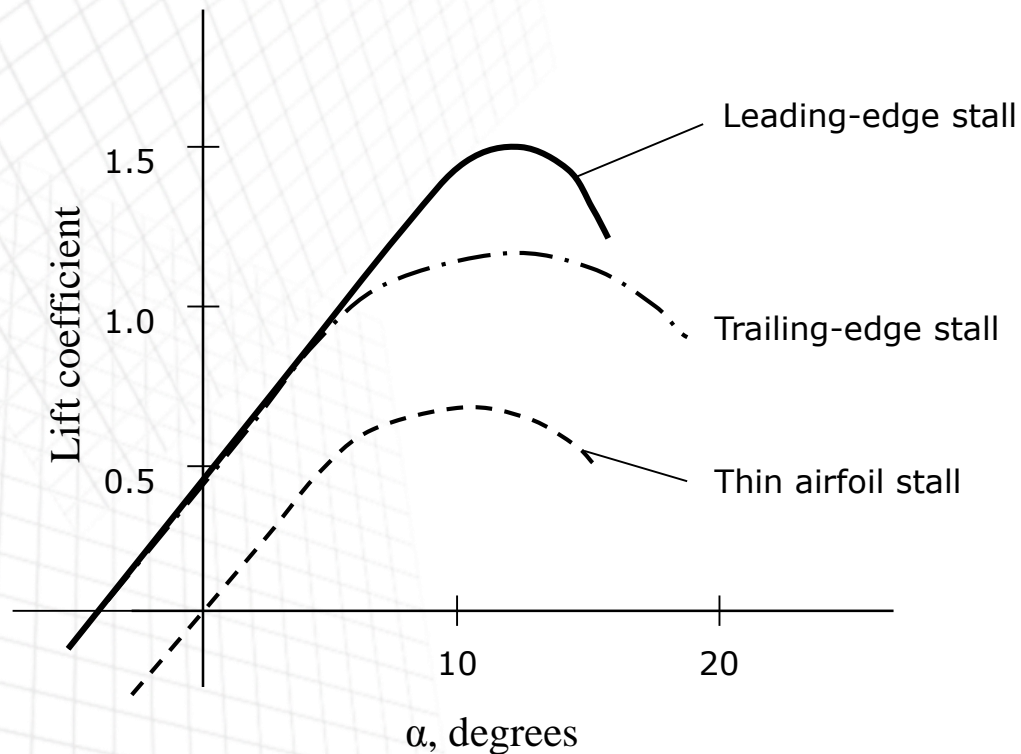
### Leading-edge stall

Flow separation takes place over the entire surface of the airfoil after occurring at the leading edge

## < 4.12 The Flow over an Airfoil – the Real Case >

### ❖ Stall

#### ● Lift-coefficient curves

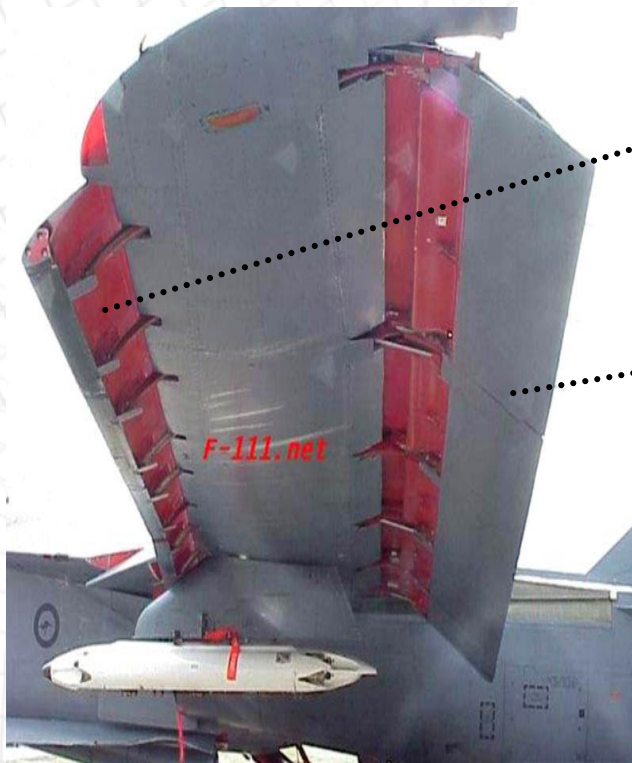




# *Incompressible Flow over Airfoils*

## < 4.12 The Flow over an Airfoil – the Real Case >

### ❖ High-lift devices



Leading edge slat

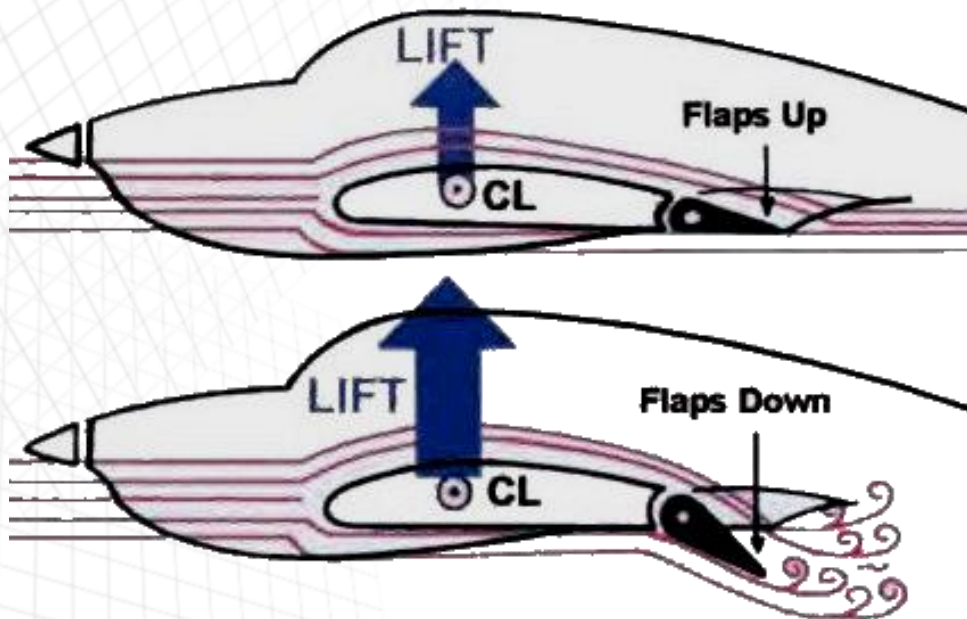
Trailing edge flap

# Incompressible Flow over Airfoils

## < 4.12 The Flow over an Airfoil – the Real Case >

### ❖ High-lift devices

- Trailing-edge flap (plain type)



More camber → Higher lift

# Incompressible Flow over Airfoils

## < 4.12 The Flow over an Airfoil – the Real Case >

### ❖ High-lift devices

- Effect of slats and flaps

